

1. First of all I must note that formula (6.135) on page 51 of Your book is right IMHO if we divide it by $\sigma y \sqrt{T_e - t}$: supposing $S_t = S_0 \exp(\sigma(\lambda t + W_t))$, where $\lambda = \frac{\mu}{\sigma} - \frac{\sigma}{2}$, we get

$$p_{S_{T_e}}(y; S_t) = \frac{d}{dy} \mathbb{P} \left(S_{T_e} \leq y \mid L < \min_{u \in [t, T_e]} S_u \leq \max_{u \in [t, T_e]} S_u < H ; S_t \right) \quad (1)$$

$$= \frac{d}{dy} \mathbb{P} \left(\widetilde{W}_{T_e - t}^\lambda \leq \frac{1}{\sigma} \ln \frac{y}{S_t} \mid \frac{1}{\sigma} \ln \frac{L}{S_t} < \min_{u \in [0, T_e - t]} \widetilde{W}_u^\lambda \leq \max_{u \in [0, T_e - t]} \widetilde{W}_u^\lambda < \frac{1}{\sigma} \ln \frac{H}{S_t} ; S_t \right) \quad (2)$$

$$= \frac{1}{\sigma y} k_{T_e - t}^\lambda \left(\frac{1}{\sigma} \ln \frac{y}{S_t} \right) = \frac{1}{\sigma y} k_{T_e - t} \left(\frac{1}{\sigma} \ln \frac{y}{S_t} \right) \exp \left(-\frac{1}{2} \lambda^2 (T_e - t) + \frac{\lambda}{\sigma} \ln \frac{y}{S_t} \right) \quad (3)$$

$$= \exp \left(-\frac{1}{2} \lambda^2 (T_e - t) + \frac{\lambda}{\sigma} \ln \frac{y}{S_t} \right) \times \sum_{n=-\infty}^{\infty} \frac{1}{\sigma y \sqrt{2\pi(T_e - t)}} \left[\exp \left(-\frac{\left(\ln \frac{y}{S_t} + 2n \ln \frac{H}{L} \right)^2}{2\sigma^2(T_e - t)} \right) - \exp \left(-\frac{\left(\ln \frac{H^2}{y S_t} + 2n \ln \frac{H}{L} \right)^2}{2\sigma^2(T_e - t)} \right) \right]. \quad (4)$$

2. The second point is that the notation (6.142) of A_K is really wrong. There should be K instead of L . Moreover IMHO I found more misprints... Take a look, e.g. for the call:

$$\nu(t) = e^{-rT_e(T_e - t)} \mathbb{E}^t(S_{T_e} - K) \mathbb{I}_{[K, H]}(S_{T_e}) \mathbb{I}_{\{L < \min_{u \in [t, T_e]} S_u \leq \max_{u \in [t, T_e]} S_u < H\}} \quad (5)$$

$$= e^{-rT_e(T_e - t)} \int_K^H (y - K) p_{S_{T_e}}(y; t) dy = e^{-rT_e(T_e - t)} \sum_{n=-\infty}^{\infty} (S_t [Q_1^n - Q_2^n] - K [P_1^n - P_2^n]) \quad (6)$$

Then we can write the following expressions for $Q_{1,2}^n$:

$$Q_1^n = \frac{1}{\sigma S_t \sqrt{2\pi(T_e - t)}} \int_K^H \exp \left(-\frac{1}{2} \lambda^2 (T_e - t) + \frac{\lambda}{\sigma} \ln \frac{y}{S_t} - \frac{\left(\ln \frac{y}{S_t} + 2n \ln \frac{H}{L} \right)^2}{2\sigma^2(T_e - t)} \right) dy \quad (7)$$

$$\left| \begin{array}{ll} x \triangleq \frac{\ln \frac{y}{S_t}}{\sigma \sqrt{T_e - t}} & y = S_t e^{\sigma \sqrt{T_e - t} x} \quad H \rightarrow A_H \\ dy = \sigma \sqrt{T_e - t} S_t e^{\sigma \sqrt{T_e - t} x} dx & K \rightarrow A_K \end{array} \right| \quad (8)$$

$$= \frac{1}{\sqrt{2\pi}} \int_{A_K}^{A_H} \exp \left(-\frac{1}{2} \lambda^2 (T_e - t) + (\sigma + \lambda) \sqrt{T_e - t} x - \frac{1}{2} (x + 2n A_{LH})^2 \right) dx \quad (9)$$

$$= \frac{1}{\sqrt{2\pi}} \int_{A_K}^{A_H} \exp \left(-\frac{1}{2} \left[(x + 2n A_{LH})^2 - 2(\sigma + \lambda) \sqrt{T_e - t} (x + 2n A_{LH}) + (\sigma + \lambda)^2 (T_e - t) \right] \right) \times \exp \left(-2n(\sigma + \lambda) \sqrt{T_e - t} A_{LH} + \frac{1}{2} (\sigma + \lambda)^2 (T_e - t) - \frac{1}{2} \lambda^2 (T_e - t) \right) dx \quad (10)$$

$$= \exp \left(-2n(\sigma + \lambda) \sqrt{T_e - t} A_{LH} + \underbrace{\sigma \left(\frac{\sigma}{2} + \lambda \right)}_{//} (T_e - t) \right) \frac{1}{\sqrt{2\pi}} \int_{A_K}^{A_H} e^{-\frac{1}{2} [x + 2n A_{LH} - (\sigma + \lambda) \sqrt{T_e - t}]^2} dx \quad (11)$$

$$= \exp \left(-2n(\sigma + \lambda) \sqrt{T_e - t} A_{LH} + \mu (T_e - t) \right) \times \left[\mathcal{N} \left(A_H + 2n A_{LH} - (\sigma + \lambda) \sqrt{T_e - t} \right) - \mathcal{N} \left(A_K + 2n A_{LH} - (\sigma + \lambda) \sqrt{T_e - t} \right) \right]. \quad (12)$$

$$Q_2^n = \frac{1}{\sigma S_t \sqrt{2\pi(T_e - t)}} \int_K^H \exp \left(-\frac{1}{2} \lambda^2 (T_e - t) + \frac{\lambda}{\sigma} \ln \frac{y}{S_t} - \frac{\left(\ln \frac{H^2}{y S_t} + 2n \ln \frac{H}{L} \right)^2}{2\sigma^2(T_e - t)} \right) dy \quad (13)$$

$$= \frac{1}{\sqrt{2\pi}} \int_{A_K}^{A_H} \exp \left(-\frac{1}{2} \lambda^2 (T_e - t) + (\sigma + \lambda) \sqrt{T_e - t} x - \frac{1}{2} (-x + 2A_H + 2nA_{LH})^2 \right) dx \quad (14)$$

$$= \exp \left(2(\sigma + \lambda) \sqrt{T_e - t} (nA_{LH} + A_H) + \sigma \left(\frac{\sigma}{2} + \lambda \right) (T_e - t) \right) \times \frac{1}{\sqrt{2\pi}} \int_{A_K}^{A_H} \exp \left(-\frac{1}{2} \left[x - 2A_H - 2nA_{LH} - (\sigma + \lambda) \sqrt{T_e - t} \right]^2 \right) dx \quad (15)$$

$$= \exp \left(2(\sigma + \lambda) \sqrt{T_e - t} (nA_{LH} + A_H) + \mu (T_e - t) \right) \times \left[\mathcal{N} \left(-A_H - 2nA_{LH} - (\sigma + \lambda) \sqrt{T_e - t} \right) - \mathcal{N} \left(A_K - 2A_H - 2nA_{LH} - (\sigma + \lambda) \sqrt{T_e - t} \right) \right]. \quad (16)$$

P_1^n and P_2^n are the same as Yours in (6.148)–(6.149). The same problem we have in the case of put. Moreover I want to say that the derivation above looks clear as well as the fact that the expression $\sigma + \lambda = \sigma + \frac{\mu}{\sigma} - \frac{\sigma}{2} = \frac{\mu}{\sigma} - \frac{\sigma}{2}$ is very natural for such formulas!